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### PV FUNDAMENTALS

- Semiconductor basics
- pn junction
- Solar cell operation
- Design of silicon solar cell

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### SEMICONDUCTOR BASICS

- Allowed energy bands
- Valence and conduction band
- Fermi level

Metal      Insulator      Semiconductor

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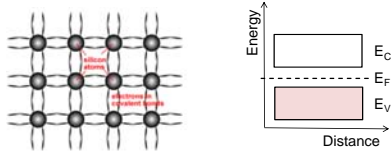
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## SEMICONDUCTOR BASICS

- Allowed energy bands
- Valence and conduction band
- Fermi level




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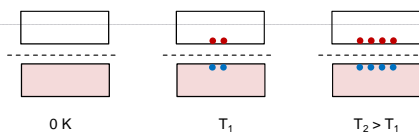
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## SEMICONDUCTOR BASICS

- Effect of temperature




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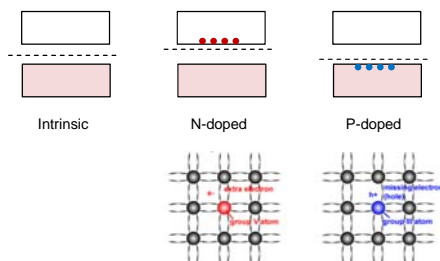
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## SEMICONDUCTOR BASICS

- Effect of doping




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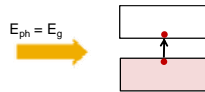
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## SEMICONDUCTOR BASICS

- **Absorption of light** depends on the energy of the photon (wavelength)



$$E = \frac{hc}{\lambda}$$

$$E(eV) = \frac{1.24}{\lambda(\mu m)}$$

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## SEMICONDUCTOR BASICS

- **Absorption of light** depends on the energy of the photon (wavelength)



$$E = \frac{hc}{\lambda}$$

$$E(eV) = \frac{1.24}{\lambda(\mu m)}$$

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## SEMICONDUCTOR BASICS

- **Absorption of light** depends on the energy of the photon (wavelength)



$$E = \frac{hc}{\lambda}$$

$$E(eV) = \frac{1.24}{\lambda(\mu m)}$$

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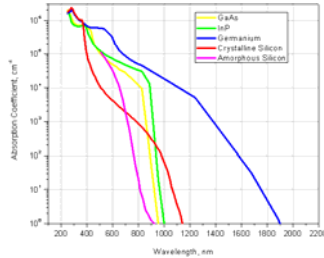
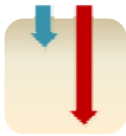
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## SEMICONDUCTOR BASICS

- **Absorption coefficient** [ $\text{cm}^{-1}$ ]: the distance into the material at which the light drops to about  $1/e$  of its original intensity

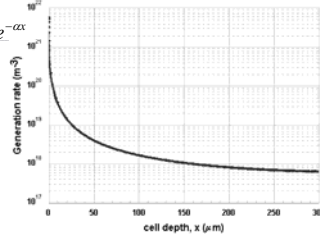
$$I = I_0 e^{-\alpha x}$$



## PV FUNDAMENTALS

- The **generation rate** gives the number of electrons generated at each point in the device due to the absorption of photons.

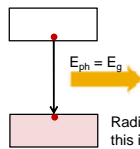
$$G = \frac{dI}{dx} = \alpha N_0 e^{-\alpha x}$$



## PV FUNDAMENTALS

**Recombination** may occur through...

- **Radiative recombination** - an electron directly combines with a hole in the conduction band and releases a photon

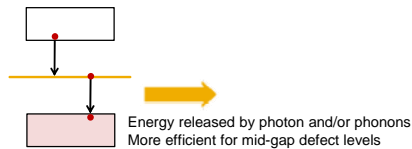


Radiated photon is weakly absorbed;  
this is how LEDs work!!  
Not very likely for indirect gap semiconductor like Si

## SEMICONDUCTOR BASICS

**Recombination** may occur through...

- **Shockley-Read-Hall recombination** – 2-step process: an electron is trapped in a defect level




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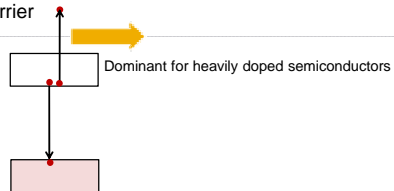
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## SEMICONDUCTOR BASICS

**Recombination** may occur through...

- **Auger recombination** – similar to radiative recombination but energy release through a third carrier




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## SEMICONDUCTOR BASICS

**Recombination** is characterized by...

- **Recombination rate**
- Minority carrier **lifetime** – how long a carrier is likely to stay around for before recombining
- **Diffusion length** – average distance a carrier can move from point of generation until it recombines

$$\tau = \frac{\Delta n}{R} \quad L = \sqrt{D\tau}$$

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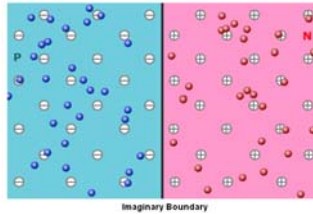
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## PN JUNCTION




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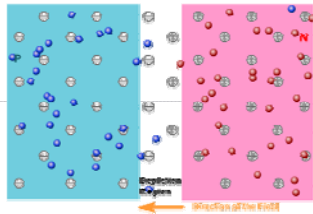
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## PN JUNCTION




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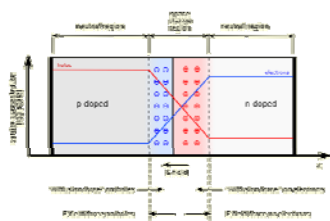
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## PN JUNCTION




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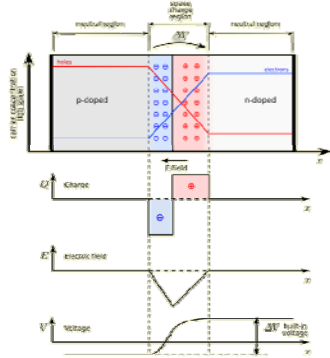
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## PN JUNCTION




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## SOLAR CELL OPERATION

### Basic steps:

- the **generation** of light-generated carriers;
- the **collection** of the light-generated carries to generate a current;
- the generation of a **voltage** across the solar cell; and
- the dissipation of power in the **load** and in parasitic resistances.

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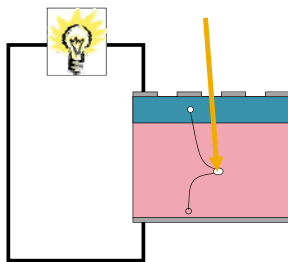
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## SOLAR CELL OPERATION




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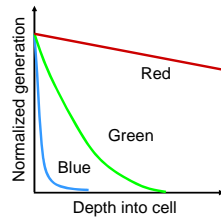
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## SOLAR CELL OPERATION

### Basic steps:

- the **generation** of light-generated carriers




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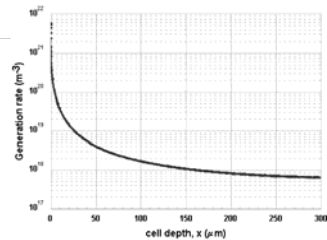
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## SOLAR CELL OPERATION

### Basic steps:

- the **generation** of light-generated carriers




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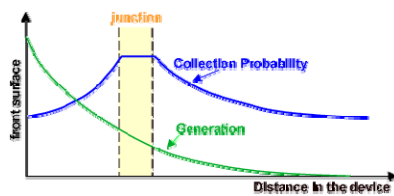
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## SOLAR CELL OPERATION

### Basic steps:

- the **collection** of the carriers




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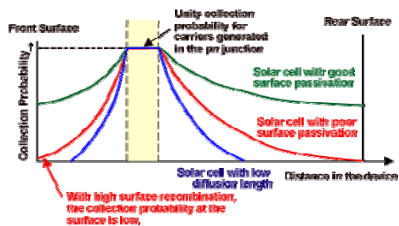
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## SOLAR CELL OPERATION

### Basic steps:

- the collection of the carriers




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## Solar cell operation

### Quantum efficiency

Ratio of the number of carriers collected to the number of photons of a given energy incident

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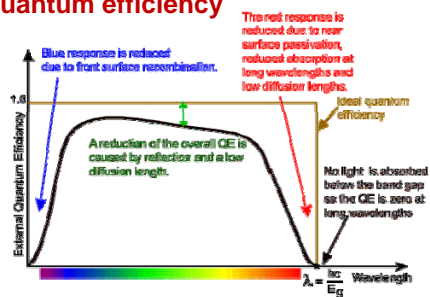
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## Solar cell operation

### Quantum efficiency



External quantum efficiency includes the effect of optical losses, e.g. reflection on the surface, ...

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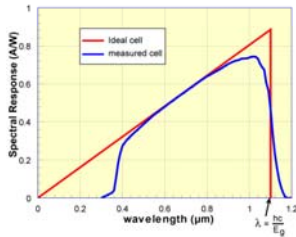
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## SOLAR CELL OPERATION

### Spectral response

Ratio of the **current** generated by the solar cell to the **power** incident on the solar cell



Spectral Response (SR) is measured

Quantum Efficiency (QE) is calculated from SR:

$$SR = \frac{q\lambda}{hc} QE$$

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## SOLAR CELL OPERATION

Solar cell parameters

### IV characteristic

= diode + light generated current

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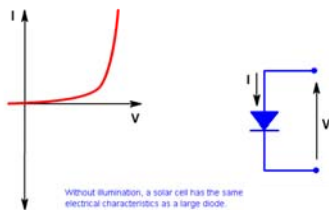
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## SOLAR CELL OPERATION

Solar cell parameters

### IV characteristic




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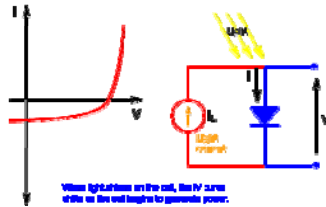
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## SOLAR CELL OPERATION

Solar cell parameters

### IV characteristic




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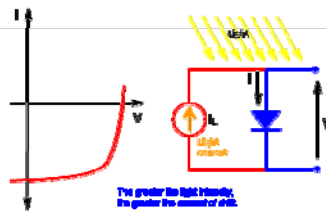
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## SOLAR CELL OPERATION

Solar cell parameters

### IV characteristic




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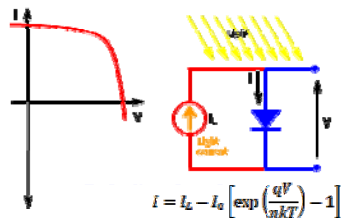
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## SOLAR CELL OPERATION

Solar cell parameters

### IV characteristic




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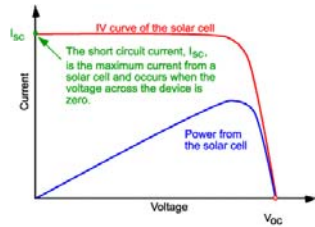
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## SOLAR CELL OPERATION

Solar cell parameters

IV characteristic: **Short Circuit Current** ( $I_{sc}$ )




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## SOLAR CELL OPERATION

Solar cell parameters

IV characteristic: **Short Circuit Current** ( $I_{sc}$ )

- Area of the solar cell (common to use  $J_{sc}$  in  $\text{mA}/\text{cm}^2$ )
- Incident flux (i.e. number of photons)
- Spectrum incident light
- Optical properties of the solar cell
- Collection probability, e.g. diffusion length

$$I_{sc} = qG(L_n + L_p)$$

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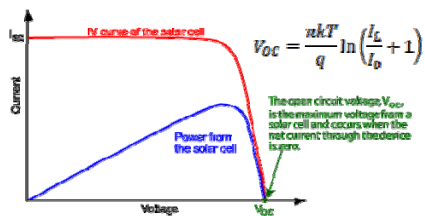
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## SOLAR CELL OPERATION

Solar cell parameters

IV characteristic: **Open circuit voltage** ( $V_{oc}$ )



$V_{oc}$  depends strongly on the recombination

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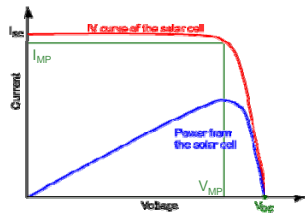
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## SOLAR CELL OPERATION

Solar cell parameters

IV characteristic: **Maximum power**




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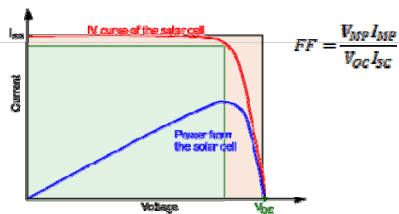
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## SOLAR CELL OPERATION

Solar cell parameters

IV characteristic: **Fill factor (FF)**




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## SOLAR CELL OPERATION

Solar cell parameters

**Efficiency ( $\eta$ )** is the fraction of incident power which is converted to electricity

$$P_{max} = V_{oc} I_{sc} FF \quad \eta = \frac{V_{oc} I_{sc} FF}{P_{in}}$$

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## SOLAR CELL OPERATION

Solar cell parameters

### Resistive effects

- Characteristic resistance
- Parasitic resistance

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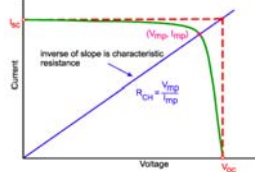
## SOLAR CELL OPERATION

Solar cell parameters

### Resistive effects

- Characteristic resistance

Maximum power transfer is  $R_{LOAD} = R_{CH}$



$$R_{CH} = \frac{V_{MP}}{I_{MP}} = \frac{V_{OC}}{I_{SC}}$$

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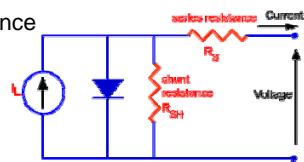
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## SOLAR CELL OPERATION

Solar cell parameters

### Resistive effects

- Characteristic resistance
- Parasitic resistance
  - Series resistance
  - Shunt resistance




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## SOLAR CELL OPERATION

Solar cell parameters

### Resistive effects

- Characteristic resistance
- **Parasitic resistance**
  - Series resistance
  - Shunt resistance

$$I = I_L - I_0 \exp \left[ \frac{q(V - IR_s)}{nkT} \right] - \frac{V + IR_s}{R_{sh}}$$

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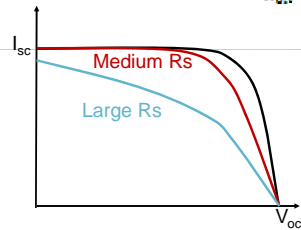
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## SOLAR CELL OPERATION

Effect of the **series resistance**

$$FF' = FF(1 - r_s) \quad \text{with } r_s = \frac{R_s}{R_{CN}}$$



Slope of the I-V curve near  $V_{oc}$  gives indication about  $R_s$

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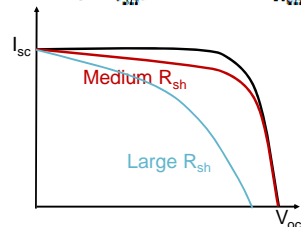
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## SOLAR CELL OPERATION

Effect of the **shunt resistance**

$$FF_{sh} = FF_0 \left( 1 - \frac{1}{r_{sh}} \right) \quad \text{with } r_{sh} = \frac{R_{sh}}{R_{CN}}$$



Slope of the I-V curve near  $I_{sc}$  gives indication about  $R_{sh}$

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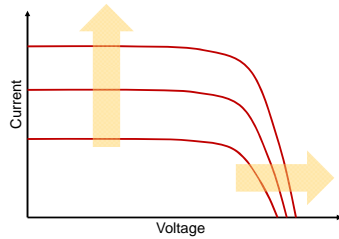
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## SOLAR CELL OPERATION

Effect of **irradiation**



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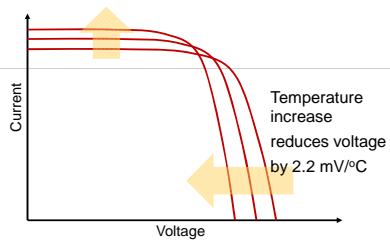
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## SOLAR CELL OPERATION

Effect of **temperature**



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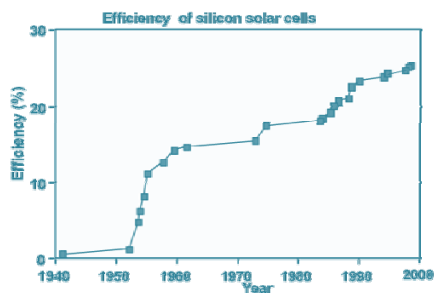
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## DESIGN OF Si SOLAR CELL



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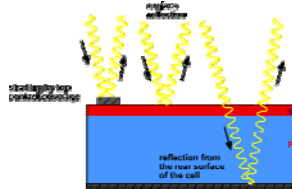
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## DESIGN OF Si SOLAR CELL

**Optical losses** - light which could have generated an electron-hole pair, but does not, because the light is reflected from the front surface, or because it is not absorbed in the solar cell.




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## DESIGN OF Si SOLAR CELL

**Optical losses** - light which could have generated an electron-hole pair, but does not, because the light is reflected from the front surface, or because it is not absorbed in the solar cell.

- Top contact shading
- Top surface reflection
- Not enough optical path for photon absorption

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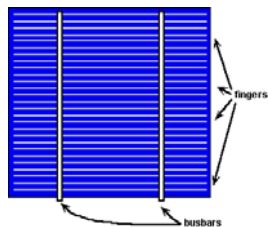
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## DESIGN OF Si SOLAR CELL

**Optical losses**  
Reduce **shading** from top contacts




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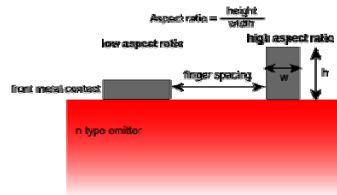
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## DESIGN OF Si SOLAR CELL

### Optical losses

Reduce **shading** from top contacts




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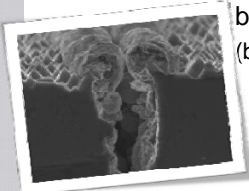
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## DESIGN OF Si SOLAR CELL

### Optical losses

Reduce **shading** from top contacts

- May increase series resistance
- Other emitter contact concepts becoming fashionable (buried or back contacts)




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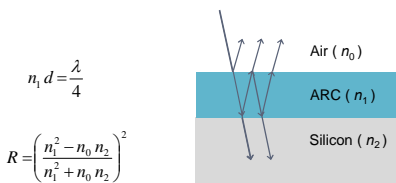
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## DESIGN OF Si SOLAR CELL

### Optical losses

Anti-reflective coating



$$n_1 d = \frac{\lambda}{4}$$

$$R = \left( \frac{n_1^2 - n_0 n_2}{n_1^2 + n_0 n_2} \right)^2$$

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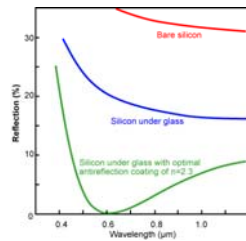
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## DESIGN OF Si SOLAR CELL

### Optical losses

#### Anti-reflective coating



## DESIGN OF Si SOLAR CELL

### Optical losses

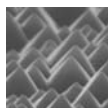
#### Surface **texturing**



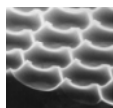
## DESIGN OF Si SOLAR CELL

### Optical losses

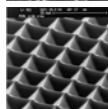
#### Surface **texturing**



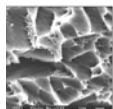
Single crystal:  
Random pyramids,  
by etching



Multi crystal:  
texturing by  
photolithography



Single crystal:  
Inverted pyramids,  
by etching

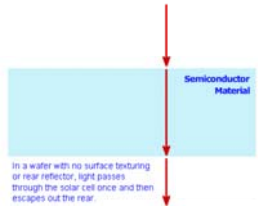


Multi crystal:  
texturing by  
macroporous  
silicon

## DESIGN OF Si SOLAR CELL

### Optical losses

Light **trapping**: increase optical length




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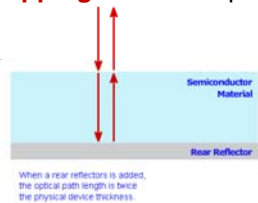
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## DESIGN OF Si SOLAR CELL

### Optical losses

Light **trapping**: increase optical length




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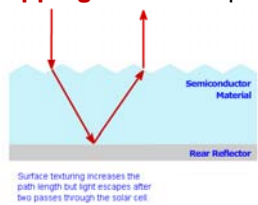
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## DESIGN OF Si SOLAR CELL

### Optical losses

Light **trapping**: increase optical length



Snell's law of refraction:  $n_1 \sin \theta_1 = n_2 \sin \theta_2$

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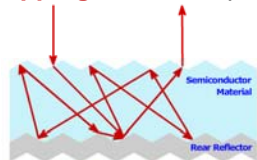
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## DESIGN OF Si SOLAR CELL

### Optical losses

Light **trapping**: increase optical length



Front and rear surface texturing can trap light for multiple passes due to total internal reflection.

Snell's law of refraction:  $n_1 \sin \theta_1 = n_2 \sin \theta_2$

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## DESIGN OF Si SOLAR CELL

### Optical losses

In summary:

- Reduce front contact coverage
- Anti-reflective coating
- Surface texturing
- Light trapping

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## DESIGN OF Si SOLAR CELL

### Recombination losses

Optimal conditions:

- the carrier must be generated within a **diffusion length** of the junction;
- the carrier must be generated closer to the junction than to *hazardous* recombination sites (**unpassivated** surface, grain boundary,...)

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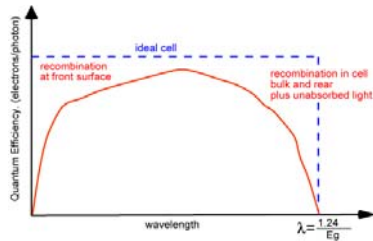
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## DESIGN OF Si SOLAR CELL

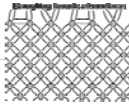
### Recombination losses



## Design of silicon solar cells

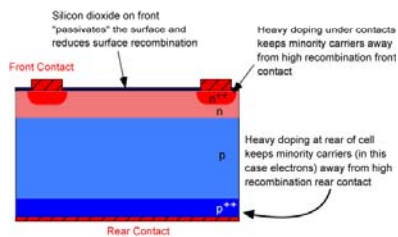
### Recombination losses: Surface **passivation**

- Reducing the number of **dangling bonds** by growing a  $\text{SiO}_2$  or  $\text{SiN}$  thin film on the surface (also for anti-reflection coating; notice that it is an electric insulator)
- Increasing doping, creating a **repelling field** (decreases diffusion length thus not suitable for charge collection region; useful closer to contacts, e.g. **Back Surface Field - BSF**)



## Design of silicon solar cells

### Recombination losses: Surface **passivation**



## DESIGN OF Si SOLAR CELL

### Single junction silicon solar cell

- Best **lab** cell: 25%

J. Zhao *et al* Novel 19.8% efficient "honeycomb" textured multicrystalline and 24.4% monocrystalline silicon solar cells. Applied Physics Letters 1998; 73: 1991–1993.

- Best **module**: 23%

M. Green *et al* Solar Cell Efficiency Tables (Version 34) Prog. Photovolt: Res. Appl. 2009; 17:320–326

- Practical cell design (for **industry**!) requires compromises, and thus lower efficiencies...

Check February issue of Photon International

Table I. Confirmed terrestrial cell and submodule efficiencies measured under the global AM1.5 spectrum (1000 W/m<sup>2</sup>) at 25 °C (IEC 60904-3: 2008, ASTM G-173-03 global)

Classification <sup>a</sup>	Effic. <sup>b</sup> (%)	Area <sup>c</sup> (cm <sup>2</sup> )	V <sub>oc</sub> (V)	J <sub>sc</sub> (mA/cm <sup>2</sup> )	FF <sup>d</sup> (%)	Test centre <sup>e</sup> (and date)	Description
<b>Silicon</b>							
Si (crystalline)	24.7 ± 0.5	4.0 (da)	0.704	42.0	83.5	Sandia (2009) <sup>f</sup>	UNSW PERL, SEH MCZ substrate <sup>28</sup>
Si (multicrystalline)	23.9 ± 0.5	22.1 (da)	0.704	41.9	81.0	Sandia (2006) <sup>g</sup>	UNSW PERL, FZ substrate <sup>29</sup>
Si (thin film transfer)	16.7 ± 0.4	4.017 (ap)	0.645	33.0	78.2	FG-ISE (2011) <sup>j</sup>	U. Stuttgart (45 µm thick) <sup>13</sup>
Si (thin film submodule)	10.5 ± 0.3	94.0 (ap)	0.492 <sup>h</sup>	29.7 <sup>h</sup>	72.1	FG-ISE (2007) <sup>j</sup>	CSG Solar (1–2 µm on glass; 20 cells) <sup>14</sup>

Table II. Confirmed terrestrial module efficiencies measured under the global AM1.5 spectrum (1000 W/m<sup>2</sup>) at a cell temperature of 25 °C (IEC 60904-3: 2008, ASTM G-173-03 global)

Classification <sup>a</sup>	Effic. <sup>b</sup> (%)	Area <sup>c</sup> (cm <sup>2</sup> )	V <sub>oc</sub> (V)	J <sub>sc</sub> (mA/cm <sup>2</sup> )	FF <sup>d</sup> (%)	Test centre <sup>e</sup> (and date)	Description
Si (large crystalline)	23.0 ± 0.5	100.4 (t)	0.729	39.6	80.0	AIST (2008)	Sanyo HIT, n-type substrate <sup>8</sup>
Si (large crystalline)	22.0 ± 0.7	147.4 (t)	0.677	40.3	80.6	FG-ISE (2006) <sup>g</sup>	Sunpower n-type substrate <sup>27</sup>
Si (large multicrystalline)	18.7 ± 0.5	217.4 (t)	0.639	37.7	77.6	AIST (2008) <sup>g</sup>	Mitsubishi Electric, honeycomb <sup>30</sup>

Table III. "Notable Exceptions": "Top ten" confirmed cell and module results, not class records measured under the global AM1.5 spectrum (1000 W/m<sup>2</sup>) at 25 °C (IEC 60904-3: 2008, ASTM G-173-03 global)

Classification <sup>a</sup>	Effic. <sup>b</sup> (%)	Area <sup>c</sup> (cm <sup>2</sup> )	V <sub>oc</sub> (V)	J <sub>sc</sub> (mA/cm <sup>2</sup> )	FF <sup>d</sup> (%)	Test centre <sup>e</sup> (and date)	Description
<b>Cells (silicon)</b>							
Si (MCZ crystalline)	24.7 ± 0.5	4.0 (da)	0.704	42.0	83.5	Sandia (2009) <sup>f</sup>	UNSW PERL, SEH MCZ substrate <sup>28</sup>
Si (moderate area)	23.9 ± 0.5	22.1 (da)	0.704	41.9	81.0	Sandia (2006) <sup>g</sup>	UNSW PERL, FZ substrate <sup>29</sup>
Si (large crystalline)	23.0 ± 0.5	100.4 (t)	0.729	39.6	80.0	AIST (2008)	Sanyo HIT, n-type substrate <sup>8</sup>
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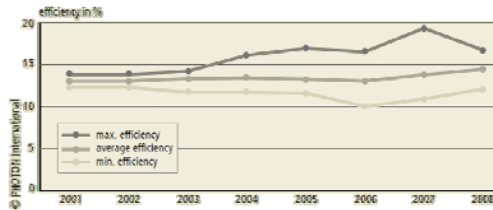
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## DESIGN OF Si SOLAR CELL

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## Next class...

- How to **make** a practical photovoltaic module
- Other** (non-silicon) technologies

And a new set of **exercises**...

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